

GENERATING TESTS FOR COMMUNICATION SOFTWARE MODELED BY PARTIALLY-SPECIFIED FINITE STATE MACHINES¹

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ABSTRACT In order to test the control portion of communication software, specifications are usually first abstracted to state machines, then test cases are generated from the resulting machines. In practical applications, the state machines obtained from the specifications are often partially-specified, and sometimes nondeterministic. We come out with two methods for test generation. The first generates test suites for the software that is modeled by partially-specified finite state machines (PFSMs) with respect to a conformance relation, called *quasi-equivalence*. The method is a generalized version of the Wp-method and applicable also to completely-specified deterministic machines which are specific class of PFSMs. This method yields usually smaller test suites with full fault coverage for each class of machines than the existing methods for the same class which also assure full fault coverage. The second method generates test suites to test deterministic implementations against their partially-specified nondeterministic finite state machine (PNFSM) specifications, with respect to a conformance relation, which we call *determinization relation*.

KEYWORDS: Error detection, finite state machines, partially-specified nondeterministic finite state machines, protocol conformance testing, and software testing.

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1. INTRODUCTION

In the area of communication software, systematic approaches have been developed for protocol conformance testing [Rayn87, Boch89], and the selection of appropriate test suites [Fuji91, Pitt90, Sidh89, Sari87, Chow78]. These approaches can produce significant economic benefits [Aho90, AT&T90]. Usually, the specifications of communication software are first abstracted to state machines, then test cases are generated from the resulting machines [Lee91, Roug89]. A considerable amount of work has been done to generate test cases for *completely-specified, deterministic* finite state machines (FSMs) [Fuji91, Sidh89, Sari84, Chow78, Gone70, Vuon89, Sabn85, Nait81, Vasi73]. However, the specifications of communication software are often *partially* (or incompletely) specified, and may be *nondeterministic*. For example, communication protocols are often partially specified [Sari84]. A major specification language for communication software, ESTELLE [Budk87, ISO9074] supports the description of partially-specified behavior. Furthermore, in practical applications, specifications may be nondeterministic but their implementations are deterministic. In nondeterministic state machine specifications, for a given state, several transitions may be associated with the same input, and they represent several choices which valid implementations can have. During implementation process, only one of the choices (transitions) is required to be implemented. Such an implementation process is also called determinization process. Some work has been reported on test generation for partially-specified deterministic machines [Petr91, Evtu89]; however, no test generation method has been reported for checking nondeterministic specifications against their implementations.

We study in this paper test generation for the finite state machines that could be both partially-specified and nondeterministic, guided by pre-defined conformance relations.

In the area of protocol conformance testing, the meaning of conformance between a specification and the valid implementations is specified either by informal description, or by precisely-defined conformance relations. Usually, the formally-defined conformance relations are preferable since they provide a means to direct the development of test generation methods and a basis to analyze the

validity of the methods. For completely-specified deterministic finite state machines (FSMs), partially-specified deterministic finite state machines (PFSMs), there are commonly-defined conformance relations in the literature [Fuji91, Chow78, Vasi73, Star72, Gill62]. However, no conformance relation has been reported for partially-specified nondeterministic finite state machines (PNFSMs), except for some general study on the specialization of object behaviors and requirement specifications [Boch92].

In Section 2, after formally defining PNFSMs and several related notations, we first describe a conformance relation, called *quasi-equivalence*, for PFSMs [Gill62]. We then introduce a conformance relation between PNFSM specifications and their PFSM implementations, called *determinization* relation. The relation is defined in terms of input/output traces in accordance with black-box testing strategy. When the relation is applied to FSM and PFSM specifications, which are specific cases of PNFSMs, it coincides to the corresponding conformance relations given in the literature. We also define several concepts which are related to test generation.

Guided by the conformance relations, in Section 3, we come out with two test generation methods. The first method is to generate test suites from PFSMs (partially-specified *deterministic* finite state machines); and the resulting test suites can be used to test PFSM implementations against their specifications with respect to the quasi-equivalence relation. The method is a generalized version of the Wp-method [Fuji91], obtained by combining the ideas given in [Fuji91] and [Evtu89]. The second one is to adaptively generate test suites from so-called *observable* PNFSMs for testing the determinization relation. The OPNFSMs have the property that a state and an input/output pair uniquely determine the next state, while a state and an input alone do not necessarily determine a unique next state and an output. The OPNFSMs are a specific class of PNFSMs that have a lower degree of nondeterminism.

In Section 4, we compare our methods with other test generation methods, on the basis of applicability, fault coverage and the size of test suites. This method yields usually smaller test suites with full fault

coverage for each class of machines than the existing methods for the same class which also assure full fault coverage.

We conclude in Section 5 by discussing some extreme case of the length of test cases and the upper bound of the size of test suites, for partial machines.

2. NOTATIONS AND ABSTRACT TESTING FRAMEWORK

We first give in this section the definition of PNFSMs, then present conformance relations between specifications and implementations under the black-box testing strategy (where implementations are assumed to be black-boxes), and finally define several concepts which are related to testing.

2.1 Partially-specified nondeterministic finite state machines (PNFSMs)

We first define PNFSMs in a traditional form similar to that given in [Star72] for NFSMs. For the convenience of presentation, we then define additional notations for PNFSMs similar to that for labeled transition systems [Brin88, Fuji91b, Fuji91c].

DEFINITION *Partially-specified Nondeterministic Finite State Machine* :

A *Partially-specified Nondeterministic Finite State Machine* (PNFSM) is defined as a 5-tuple (St, Li, Lo, h, S_0) where:

- (1) St is a finite set of states, $St = \{S_0, S_1, \dots, S_{n-1}\}$.
- (2) Li is a finite set of inputs.
- (3) Lo is a finite set of outputs.
- (4) h is a behavior function:

$$h : d \Rightarrow \text{powerset}(St \times Lo) \setminus \{\square\} \quad \text{where}$$

- (i) $d \subseteq St \times Li$ (PNFSM becomes completely specified if $d = St \times Li$);
- (ii) \square denotes the empty set.

Let $P, Q \in St$, $a \in Li$ and $b \in Lo$. We write $P \xrightarrow{a/b} Q$ to denote $(Q, b) \in h(P, a)$; $P \xrightarrow{a/b} Q$ is called a *transition* from P to Q with label a/b .

(5) S_0 is the initial state, which is in St . \square

We assume that a "reliable" reset input r is available in any implementation of a PNFSM such that upon receiving r in any state the implementation returns to the initial state.

We often use in the following the term "partial machine" to refer to a PNFSM, which may be deterministic or not. A partial machine can be represented by a directed graph in which the nodes are the states and the directed edges are transitions linking the states. Figure 1 shows an example of such a machine.

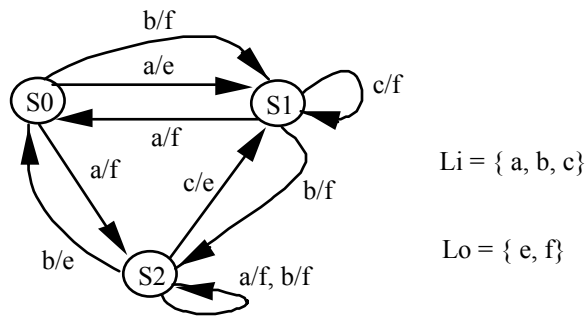


Figure 1. An example of a PNFSM

For the convenience of the presentation, we also introduce in Table 1 several notations.

Table 1. Notation for PNFSMs

notation	meaning
L	$Li \in Lo$, a set of input/output pairs; u denotes such a pair
ϵ	ϵ is the empty sequence.
L^*	set of sequences over L ; x denotes such a sequence. Note that $\epsilon \in L^*$
$P \not\xrightarrow{u} Q$	For $P, Q \in St$, not($\exists Q(P \xrightarrow{u} Q)$)
$P \xrightarrow{\epsilon} Q$	$P=Q$
$P \xrightarrow{a/b} Q$	$P \xrightarrow{a/b} Q$
$P \xrightarrow{x} Q$	$\exists P_1, \dots, P_{k-1} \in St (P=P_0 \xrightarrow{u_1} P_1 \dots \xrightarrow{u_k} P_k=Q)$ where $u_1, \dots, u_k \in L$, and $x=u_1 \dots u_k$
$P \xrightarrow{x} \rightarrow$	$\exists Q \in St (P \xrightarrow{x} Q)$
$Tr(P)$	$Tr(P) = \{ x \mid P \xrightarrow{x} \rightarrow \}$
x^{in}	For $x \in L^*$, x^{in} is an input sequence obtained by deleting all outputs in x (note that $x^{in} \in L^*$)
V^{in}	For $V \in L^*$, $V^{in} = \{ x^{in} \mid x \in V \}$

$$Tr^{in}(P) \quad Tr^{in}(P) = \{ x^{in} \mid P = x \Rightarrow \},$$

(note that $Tr^{in}(P) = Li^*$ for each state P of completely-specified NFSMs)

DEFINITION *Initially connected PNFSM:*

Given a PNFSM $S (St, Li, Lo, h, S_0)$, S is said to be *initially connected* iff

$$\forall S_i \in St \exists x \in L^* (S_0 = x \Rightarrow S_i). \quad \square$$

In initially connected PNFSMs, every state is reachable from the initial state. Without loss of generality, we assume that all machines considered in the rest of the paper are initially connected. If a given machine S is not initially connected, we may consider only such a submachine which is a portion of S consisting of all states and transitions that are reachable from the initial state of S . The unreachable states and transitions of machines do not affect the behavior.

We first define so-called *observable PNFSMs*, a concept originally described in [Star72] for completely specified machines, which represents a restricted form of nondeterminism.

DEFINITION *Observable PNFSMs (OPNFSMs) :*

A PNFSM is said to be *observable* if for every state $S \in St$, and every input/output pair $a/b \in L$, there is at most one transition; that is, $S - a/b \rightarrow S_1 \ \& \ S - a/b \rightarrow S_2 \implies S_1 = S_2$. \square

As an example, Figure 1 shows an OPNFSM. OPNFSMs are a subclass of partial machines. In observable machines, a state and an input/output pair can uniquely determine at most one next state. However, an OPNFSM may still be nondeterministic in the sense that a state and an input cannot determine a unique next state and a unique output. We note that all deterministic machines are observable.

Given a state P in a PNFSM, we say that P is *deterministic* if no two outgoing transitions from P have the same input; and we say that P is *nondeterministic* if P is not deterministic. For a PNFSM, if every state is deterministic, then the machine is deterministic; and we call it a partial FSM

(PFSM). We now define in the following several specific classes of PFSMs, which are useful concepts for test generation.

DEFINITION: *Reduced PFSMs* :

An PFSM is *reduced* iff $\forall S_i, S_j \in St (i \neq j \implies Tr(S_i) \neq Tr(S_j))$. \square

A PFSM is reduced if and only if none of its states accept the same set of input/output sequences.

DEFINITION: *Distinguishable states*:

Given a pair of states S_i and S_j , S_i and S_j are *distinguishable*, written $S_i \neq S_j$, iff

$$\exists x \in Tr(S_i) \& Tr(S_j) (x^{in} \in Tr^{in}(S_i) \leftrightarrow Tr^{in}(S_j))$$

where $Tr(S_i) \& Tr(S_j) = (Tr(S_i) \approx Tr(S_j)) \setminus (Tr(S_i) \leftrightarrow Tr(S_j))$.

If a pair of states are not distinguishable, we say that they are *indistinguishable*. \square

Two states are distinguishable if and only if there is an input/output sequence x such that x can be accepted by only one of the two states but the input sequence x^{in} can be accepted by the both of them.

DEFINITION: *Minimal PFSMs*:

A PFSM is *minimal* iff $\forall S_i, S_j \in St (i \neq j \implies S_i \neq S_j)$. \square

A PFSM is minimal if and only if every pair of states are distinguishable.

A minimal PFSM is reduced, but a reduced PFSM is not necessarily minimal. Given a minimal machine S , each state of P is distinguishable from all other states of P , which is not necessarily true for a reduced machine. If we consider a completely specified machine, then a reduced machine is also minimal.

We also need the following concepts for presenting our method.

DEFINITION: *prefix set* $\text{pref}(V)$ for a given set of sequences:

Given a set of sequences $V \subseteq L^*$,

$$\text{pref}(V) = \{t_1 \mid t_2 \in L^* \ \& \ t_1.t_2 \in V\} \quad \text{where } t_1.t_2 \text{ is the concatenation of } t_1 \text{ with } t_2. \quad \square$$

DEFINITION: *Concatenation of sets of i/o sequences or input sequences:*

Assuming $V_1, V_2 \subseteq L^*$ (or $V_1, V_2 \subseteq L_i^*$), *the concatenation of sets*, written " \cdot ", is defined as follows:

$$V_1.V_2 = \{t_1.t_2 \mid t_1 \in V_1 \ \& \ t_2 \in V_2\} \quad \text{where } t_1.t_2 \text{ is the concatenation of } t_1 \text{ with } t_2.$$

$$\text{We write } V^n = V.V^{n-1} \quad \text{for } n > 1 \quad \text{and} \quad V^1 = V. \quad \square$$

2.2. Conformance relations

Before any study on how to generate test suites, the following question must first be answered: under the black-box testing strategy, what kind of conformance relation between a specification and the corresponding implementation is expected to hold ?

For (completely-specified, deterministic) FSMs, there is a widely-accepted conformance relation, called *equivalence*, (see, e.g., [Fuji91, Chow78, Vasi73, Star72, Gill62]), which requires that a specification and its implementation produce the same output sequence for every input sequence. We define in this section conformance relations for machines in terms of the relations between their initial states.

DEFINITION *Equivalence:*

The *equivalence* relation between two states P and Q in PFSMs, written

$$P \equiv Q, \text{ holds iff } Tr(P) = Tr(Q)$$

Given two PFSMs S and I with their initial states S_0 and I_0 , we write $S \equiv I$ iff $S_0 \equiv I_0$. \square

A reduced machine has no equivalent states. For PFSMs, a conformance relation, called *quasi-equivalence*, was presented in [Gill62, Star72, Evtu89]. The relation requires that, for every input sequence that can be accepted by a specification, the specification and its implementation produce the same output sequence.

DEFINITION *Quasi-equivalence:*

The *quasi-equivalence* relation between two states P and Q in PFSMs, written

$$P \leq_{\text{quasi}} Q, \text{ holds iff } Tr(P) \equiv Tr(Q)$$

Given two PFSMs S and I with their initial states S_0 and I_0 , we write $S \leq_{\text{quasi}} I$ iff $S_0 \leq_{\text{quasi}} I_0$. \square

The quasi-equivalence relation is not an equivalent relation since it is not symmetric.

However, it is quite often in practical applications that specifications are nondeterministic and their implementations are deterministic. For a state P and a set of transitions starting from P, we say that in state P, an input a *associates* the set of transitions if the input symbol of every transition in the set is a . In nondeterministic state machine specifications, for a given state, several transitions may be associated with the same input, and they represent several choices which valid implementations can have. During implementation process, only one of the choices is required to be implemented. Such an implementation process is also called determinization process. We now formalize the conformance relation between PNFSM specifications and their PFSM implementations, which we call *determinization relation*.

DEFINITION *Choice:*

The *choice* relation between a PNFSM S and a PFSM S', written

$$S \varepsilon_{\text{cho}} S', \text{ holds iff } S' \text{ can be obtained from } S \text{ in the following fashion:}$$

For every $P \in St$ and every $a \in Li$, if the input a associates more than one transitions from the state P, keep one of them and eliminate the rest of transitions. We say that S' is *chosen* from S. \square

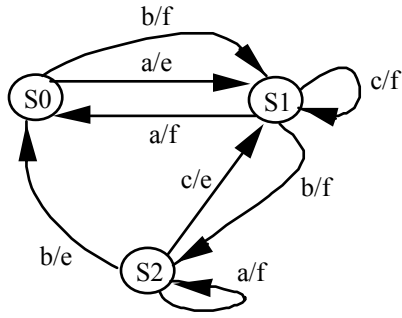


Figure 2. A PFSM chosen from the PNFSM of Figure 1

DEFINITION *Determinization*

The *determinization* relation between a PNFSM S and a PFSM I , written $S \varepsilon_{\text{det}} I$, holds iff $\exists S'(S \varepsilon_{\text{cho}} S' \ \& \ S' \leq_{\text{quasi}} I)$. \square

We present in the following the relations among the above-defined conformance relations .

THEOREM 1: Given two PNFSMs S and I , assuming that they have common L_i and L_o , we have the following statements:

- (i) $S \neq I \iff S \leq_{\text{quasi}} I \ \& \ I \leq_{\text{quasi}} S$
- (ii) if S and I are (deterministic) PFSMs, then $S \varepsilon_{\text{det}} I \iff S \leq_{\text{quasi}} I$
- (iii) if S and I are (completely-specified, deterministic) FSMs, then

$$S \leq_{\text{quasi}} I \iff S \neq I \iff S \varepsilon_{\text{det}} I. \quad \square$$

The above theorem is evident from the corresponding definitions.

2.3. Definitions related to testing

We define in this section several concepts which are related to testing finite state machines.

DEFINITION *Test case* and *test suite* :

For a given PNFSM, a sequence t of a finite length is a *test case* if $t \in \text{Tr}^{\text{in}}(S_0)$. A *test suite* is a finite set of test cases. \square

DEFINITION : *Equivalence* with respect to a given input set:

The *equivalence* relation between two states P and Q, with respect to a given input set Σ^* , written $P \equiv Q$, holds iff $\forall x \in \Sigma^* (Tr(P) \& Tr(Q) (x \in Tr^{in}(P) \leftrightarrow Tr^{in}(Q) \implies x^{in} \equiv \epsilon))$.

Given two PNFSMs S and I with their initial states S_0 and I_0 , we write $S \equiv I$ iff $S_0 \equiv I_0$. \square

The equivalence relation with respect to a given input set Σ requires that, *for every input sequence in Σ^* that can be accepted by both a specification and its implementation, the specification and its implementation produce the same output sequence.*

We note: (i) $S \not\equiv I$ iff $\exists \Sigma^* (S \not\equiv I)$, and (ii) $S \leq_{quasi} I$ iff $\forall \Sigma^* (S \equiv I)$.

3. TEST GENERATION

We present in this section two test generation methods. The first method is to generate test suites from PFSMs (partially-specified *deterministic* finite state machines); and the resulting test suites can be used to test PFSM implementations against their specifications with respect to the quasi-equivalence. The second one is to adaptively generate test suites from PNFSMs (partially-specified *nondeterministic* finite state machines) for testing the determinization relation.

3.1. Test generation for PFSMs with respect to quasi-equivalence

We first define several key concepts for presenting our method, then give an algorithm of generating test suites, and finally present a theorem for establishing the validity of the algorithm.

DEFINITION: *Characterization set* W:

Given an PFSM, a *characterization set* is a minimal set $W \in \Sigma^*$ such that:

$\forall S_i, S_j \in St (S_i \equiv S_j \implies \exists x \in \Sigma^* (Tr(S_i) \& Tr(S_j) (x^{in} \in Tr^{in}(S_i) \leftrightarrow Tr^{in}(S_j) \leftrightarrow W)))$. \square

The above definition is generalized from the concept of the characterization set for FSMs given in [Chow78] to PFSMs. We omit the algorithm for generating characterization sets because of the length limitation of the paper. One can develop such an algorithm by borrowing the ideas of generating characterization sets for FSMs pointed out by [Koha70, Chow78].

DEFINITION: *State identification sets* $\{W_0, W_1, \dots, W_{n-1}\}$:

Given a PFSM with n states and a characterization set W , $\{W_0, W_1, \dots, W_{n-1}\}$ is a tuple of *state identification sets* if, for $i=0, 1, \dots, n-1$, W_i is a minimal set such that

- (i) $W_i / Tr^{in}(S_i) \leftrightarrow pref(W)$, and
- (ii) for $j=0, 1, \dots, n-1$, $(S_i \rightarrow S_j \implies \exists x \in Tr(S_i) \& Tr(S_j) (x^{in} \in W_i))$. \square

The above definition is generalized from the concept for FSMs given in [Fuji91] to PFSMs.

DEFINITION: *subscripts(A)* for a given state set:

For $A \subseteq St$, *subscripts(A)* is a string of integers i_1, i_2, \dots, i_k ,

where $i_1 < i_2 < \dots < i_k$ and $A = \{S_{i_1}, S_{i_2}, \dots, S_{i_k}\}$. \square

Given two sets of states A and B , we say that the *subscripts* of A is *smaller* than that of B if *subscripts(A)* precedes *subscripts(B)* in lexicographic order. The notation *subscripts(A)* for a given set of states A is needed for defining a so-called *maximal set of pairwise-distinguishable states* $f(S_i)$ for a given state S_i for PFSMs. A set of states are *pairwise-distinguishable* if and only if every pair of states in the set are distinguishable. A *maximal set of pairwise-distinguishable states* is a set such that it is not contained by any other set of pairwise-distinguishable states. A maximal set of pairwise-distinguishable states $f(S_i)$ for a given state S_i is the set with the smallest subscript among the maximal sets of pairwise-distinguishable states that contains S_i , which is formally defined as follows.

DEFINITION: *Maximal set of pairwise-distinguishable states* $f(S_i)$ for a given state S_i :

Given a PFSM and a state $S_i \in St$, $f(S_i)$ is defined as a set $A \subseteq St$ such that:

(i) $S_i \in A$, and

(ii) $\forall S_k, S_j \in A$ ($k \neq j \implies S_k \not\sim S_j$), and

(iii) there is no $B \subseteq St$ such that

(i') $S_i \in B$, and

(ii') $\forall S_k, S_j \in B$ ($k \neq j \implies S_k \not\sim S_j$), and

(iii') $|B| > |A|$ or

$|B|=|A|$, and $subscripts(B)$ precedes $subscripts(A)$ in lexicographic order. \square

Given a minimal machine, for every state S_i , we have $f(S_i) = St$. For a given PFSM, we denote the number of all different maximal sets of pairwise-distinguishable states $f(S_i)$'s as *fuzziness degree* δ , as defined below.

DEFINITION: *Fuzziness degree* δ for a given PFSM:

Given a PFSM, we have $\delta = |\{f(S_i) \mid S_i \in St\}|$. \square

According to the above definition, every state S_i has only one maximal set of pairwise-distinguishable states $f(S_i)$. Therefore, it is easy to see that $1 \leq \delta \leq |St|$, and $\delta=1$ for any minimal PFSM.

DEFINITION : *Prime machine:*

For a given PFSM S (St, Li, Lo, h_S, S_0), the *prime machine* of S is a reduced (not necessarily minimal) PFSM M (St_M, Li, Lo, h_M, M_0) such that $S \neq M$. \square

We give in the following the test generation algorithm. This algorithm requires that the user previously estimates an *upper bound* on the number of states in the prime machine of the given FSM implementation, that is, the number of states in its minimal form.

ALGORITHM 1: Test generation.

Input : A specification S in the form of a (arbitrary) PFSM (St, Li, Lo, h, S_0) , and the upper bound m on the number of states in the prime machine of the given FSM implementation.

Output : a test suite \square .

Step 1: Determine the fuzziness degree δ of S .

Step 2: Let the number of states in S be n ($n \leq \delta m$). Construct a characterization set W , and a tuple of state identification sets $\{W_0, W_1, \dots, W_{n-1}\}$.

Step 3: Construct a minimal set QLi^* such that: $\forall S_i \in St \exists x \in L^* (x^{in} \in Q \ \& \ S_0 = x \Rightarrow S_i)$.

Step 4: Let $P = Q \cdot (\{\epsilon\} \approx Li)$ and $R = P \setminus Q$

Step 5: Assume: (i) for $\forall L_i^*, \forall @W = \bigcup_{S_0=x \Rightarrow S_i} \{x^{in}\} \cdot (W \leftrightarrow Tr^{in}(S_i))$.

(ii) for $\forall L_i^*, \forall \{W_0, W_1, \dots, W_{n-1}\} = \bigcup_{S_0=x \Rightarrow S_i} \{x^{in}\} \cdot W_i$

Construct a test suite \square in the following manner:

$$\square = \square_1 \approx \square_2$$

where $\square_1 = Q \cdot (\{\epsilon\} \approx Li \approx Li^2 \approx \dots \approx Li^{\delta m - n}) @ W$, and

$$\square_2 = R \cdot Li^{\delta m - n} \{W_0, W_1, \dots, W_{n-1}\}. \quad \square$$

In the above algorithm, the given specification is not required to be reduced. However, a much smaller test suite will be obtained if we use its reduced form.

For example, assuming that the implementation is a minimal FSM and will not have more than 3 states, we generate a test suite for the PFSM of Figure 2 as follows:

$$W = \{a, b\}, \quad W_0 = \{a\}, \quad W_1 = \{a, b\}, \quad W_2 = \{b\}$$

$$Q = \{\epsilon, a, a.b\}, \quad P = \{\epsilon, a, b, c, a.a, a.b, a.c, a.b.a, a.b.b, a.b.c\},$$

$$R = \{b, c, a.a, a.c, a.b.a, a.b.b, a.b.c\},$$

$$\delta = 1,$$

$$\square_1 = \{\epsilon, a, a.b\} @ \{a, b\} = \{a, b, a.a, a.b, a.b.a, a.b.b\}$$

$$\begin{aligned}
\Box 2 &= \mathbb{R}8 \{W_0, W_1, W_2\} \\
&= \{b\}.W_1 \approx \{a.a\}.W_0 \approx \{a.c\}.W_1 \approx \{a.b.a\}.W_2 \approx \{a.b.b\}.W_0 \approx \{a.b.c\}.W_1 \\
&= \{b.a, b.b, a.a.a, a.c.a, a.c.b, a.b.a.b, a.b.b.a, a.b.c.a, a.b.c.b\} \\
\Box &= \Box 1 \approx \Box 2 = \{a, b, a.a, a.b, a.b.a, a.b.b, b.a, b.b, a.a.a, a.c.a, a.c.b, a.b.a.b, \\
&\quad a.b.b.a, a.b.c.a, a.b.c.b\}
\end{aligned}$$

Furthermore, a test suite could be reduced by deleting each test case that is a prefix of another test case. The final test suite is $\{b.a, b.b, a.a.a, a.c.a, a.c.b, a.b.a.b, a.b.b.a, a.b.c.a, a.b.c.b\}$. A reset input must be sent before a test case is applied.

THEOREM 2: (Validity of the test generation method):

Consider a given specification S in the form of a PFSM, and any FSM I . Suppose $n \leq \delta m$ where n is the number of states in S , and m is the upper bound of number of states in the prime machine of I . Let \Box be the test suite generated for S using Algorithm 1. We have $S \leq_{\text{quasi}} I$ iff $S =_{\Box} I$.

Proof : The theorem follows from Lemmas given in Appendix. \square

As shown in Algorithm 1, test suites for minimal partial machines can be constructed in the same way as for completely specified minimal machines since δ is equal to one for minimal machines. However, if a partial machine has indistinguishable states, then the machine cannot be transformed into its minimal form to generate test suite with respect to the quasi-equivalence relation. The reason is that the transformation of a partial machine into a minimal form by merging states will result in the appearance of new traces that are not defined in the original machine. In turn, this results in that some valid implementations may not pass a test suite derived from the minimal form, and that some test cases in such a test suite may be not acceptable in the original machine. Therefore, partial machines should not be transformed into a minimal form for test generation.

3.2. Test generation for OPNFSMs with respect to determinization relation

We present in this section an adaptive testing procedure to generate test suites from OPNFSMs for testing the determinization relation.

ADAPTIVE TESTING PROCEDURE:

Input : An OPNFSM specification S and an FSM implementation I (the internal structure of implementation is not available).

Output : Report " $(S \varepsilon_{\text{det}} I)$ " or " $\text{not}(S \varepsilon_{\text{det}} I)$ ".

Step 1: Let an OPNFSM variable SS be S initially. If the SS is not a deterministic PFSM, then go to Step 2. Otherwise, go to Step 7.

Step 2: For the SS , find $x \in L^*$ and a nondeterministic state S_i such that

$$S_0 = x \Rightarrow S_i \text{ and } \forall y \in \text{pref}(\{x\}) (y \sqsubseteq x \ \& \ S_0 = y \Rightarrow S_j \implies S_j \text{ is deterministic.})$$

Step 3: Find $a \in L^{\text{in}}$ such that the multiplicity of the set $\{u \mid u^{\text{in}} = a \ \& \ S_i = u \Rightarrow\}$ is over one.

Step 4: Apply the test sequence $r.x^{\text{in}}.a$ to the implementation (r is the reset input). If the output sequence observed after applying $r.x^{\text{in}}$ is not the one produced by applying the test sequence to the specification, then report " $\text{not}(S \varepsilon_{\text{det}} I)$ " (i.e., the implementation fails to pass the testing), and stop.

Otherwise, assume the last output in the resulting output sequence is d , and do Step 5.

Step 5: If $\text{not}(S_i = a/d \Rightarrow)$, then report " $\text{not}(S \varepsilon_{\text{det}} I)$ ", and stop. Otherwise, do Step 6.

Step 6: Construct a new OPNFSM SS from the original by deleting all transitions from S_i with the input a except for the transition with the label a/d . If the resulting SS is not a deterministic PFSM, then go to Step 2. Otherwise, go to Step 7.

Step 7: Generate a test suite from SS using Algorithm 1, then apply the resulting test suite \square to the implementation. If $SS = \square I$, then report " $(S \varepsilon_{\text{det}} I)$ "; otherwise, report " $\text{not}(S \varepsilon_{\text{det}} I)$ ". Stop. \square

We say the above procedure to be adaptive because the test selection depends on the result of application of the formerly selected test cases. We use an example to explain the testing procedure.

Assume that the specification is the OPNFSM shown in Figure 1, and that the implementation I

satisfies $S' \leq_{\text{quasi}} I$ where S' is the PFSM shown in Figure 2. First, we find a nondeterministic state S_0 in Step 2 with $x = \epsilon$. By Steps 3 and 4, we derive a test sequence $r.a$. The last output in the resulting output sequence must be e ; then construct a new machine SS by deleting the transition from S_0 to S_2 with the label a/f . After repeating the above steps once again, we delete the transition from S_2 to S_2 with the label b/f . At this point, the resulting SS is the PFSM shown in Figure 2. According to Step 7, we generate a test suite from the SS , as shown in Section 3.1.

4. COMPARISON WITH OTHER RELATED WORK

Since FSMs and PFSMs are specific classes of OPNFSMs, our methods can be applied to them, to test the equivalence and quasi-equivalence relations, respectively (see Theorem 1). We compare in this section our method for OPNFSMs with the other test generation methods for different machines [Fuji91, Vuon89, Sabn85, Nait81, Chow78, Vasi73, Petr91, Petr92, Evtu89], which also require a "reliable" reset in the implementations (note, that simple experiments or checking sequences do not use this assumption), as shown in Figure 3. When applied to such classes of machines, this method yields usually smaller test suites with full fault coverage for each class of machines than the existing methods for the same class which also assure full fault coverage.

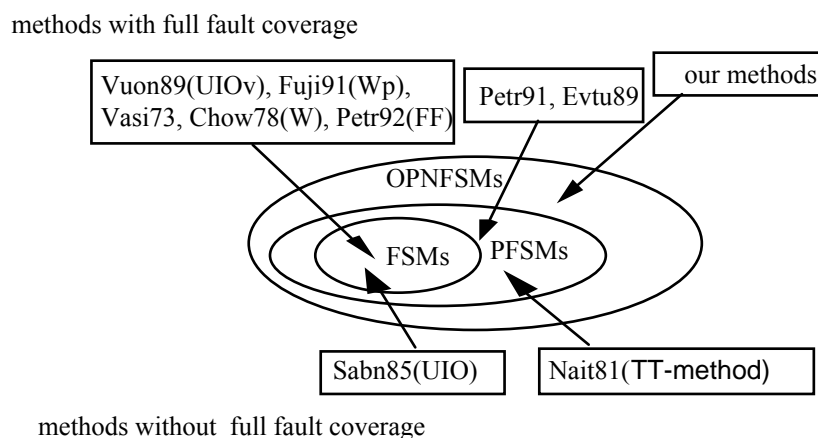


Figure 3. General comparison based on applicability and fault coverage

When our method is applied to FSMs, the conformance relation to be tested is the equivalence, the same as in the W-method [Vasi73, Chow78], the Wp-method [Fuji91], the UIO-method [Sabn85], the UIOv-method [Vuon89], the FF-method [Petr92] and the TT-method (Transition tour) [Nait81]. The UIO-method does not guarantee full fault coverage, as it has been pointed out in [Vuon89]; neither does the TT-method. These methods have been justified by simulation on the basis of percentage of fault coverage. UIOv- and FF- methods guarantee full fault coverage (i.e., check equivalence) only if no malfunction causes an increase in the number of states. The W- and Wp-methods detect all faults that may even increase the state number up to the given bound, and the latter produces, in general, smaller test suite than the former [Fuji91].

The method given in Section 3.1 may be considered a generalization of the Wp-method [Fuji91], and is, in particular, applicable to deterministic FSMs, which are a specific class of PFSMs. We note that even for FSMs, our method is slightly different from the Wp-method. We do not require WiW as in the Wp-method, instead, we only require $Wi\text{pref}(W)$. Since WiW implies $Wi\text{pref}(W)$ but not vice versa, our method may produce shorter test cases than W- and Wp-methods.

Test generation for partial FSMs has received much less attention than that for completely-specified FSMs. However, practical communication software are often modeled as partial machines. Some authors proposed to complete the "don't care" state/input combinations of partial machines in accordance with a so-called *completeness assumption* [Sabn85, Vuon89]. The assumption states that a machine should be constructed in such a way that, for every state/input combination representing "don't care", it produces a *null* or *error* output and either remains in the *same* state or goes into an *error* state. However, in many cases, implementations are not constructed in the above way. In this case, the completeness assumption cannot be satisfied. Methods for test suite generation from a deterministic partial FSM were reported in [Evtu89, Petr91]. We note that neither the method given in Section 3.1 nor method given in [Petr91] necessarily produces smaller test suites than the other. However, our methods combine the ideas given in [Evtu89] and [Fuji90], can generate usually

smaller test suites than the method given in [Evtu89], and are applicable to testing deterministic machine implementations against their nondeterministic specifications.

5. CONCLUSION

We first present in this paper a method of generating test cases from partially-specified finite state machines specifications. If a given PFSM is not minimal and its fuzziness degree δ is more than one, then the lengths of test cases produced by our method grow rapidly when δ increases. Let n and m be the numbers of states in a specification and its implementation, respectively. In the extreme case, when $\delta = n$, the length of a test case can reach n^3m , as shown in [Evtu89]. As to the multiplicity of test suites produced by the method given in Section 3.1, the order is $O(n^3|L_i|^{\delta m - n + 1})$. We then give a method of generating test suites to check OPNFSM deterministic implementations against their nondeterministic specifications. Our methods can be applied to test generation for the control portion of the software written in SDL [Beli89] or ESTELLE.

APPENDIX : VALIDITY OF TEST METHOD

For the convenience of presentation, we make several conventions and definitions; then we give several lemmas which are required for proving the Theorem 2.

Given a PFSM $S (St_S, L_i, Lo, h_S, S_0)$ and an FSM $I (St_I, L_i, Lo, h_I, I_0)$, we assume in the following:

- (1) All states of S and I are reachable from the initial states S_0 and I_0 , respectively.
- (2) S has n states with $n \geq 2$.
- (3) $M (St_M, L_i, Lo, h_M, M_0)$ is the prime machine of I , and may have at most m states with $\delta m \geq n$.
- (4) S_i, S_j, S_k, S_l , and M_i, M_j, M_k, M_l represent the states of S and M , respectively.
- (5) A characterization set is W . A tuple of state identification sets is $\{W_0, W_1, \dots, W_{n-1}\}$.
- (6) the fuzziness degree of S is δ .
- (7) a set QL_i^* constructed from S such that: $\forall S_i \in St \exists x \in L^* (x \in QL_i^* \& S_0 = x \Rightarrow S_i)$.

(8) $P=Q.(\{\varepsilon\} \approx Li)$) and $R=PQ$.

(9) A test suite \square which is constructed using Algorithm 1:

$$\square = \square 1 \approx \square 2$$

where $\square 1 = Q.(\{\varepsilon\} \approx Li \approx Li^2 \approx \dots \approx Li^{\delta m-n})@W$, and

$$\square 2 = R. Li^{\delta m-n} \{W_0, W_1, \dots, W_{n-1}\}. \quad \square$$

Definitions of several notations

notation	meaning
$[S_i, M_i] -u-> [S_j, M_j]$	For $u \in L$, $S_i -u-> S_j$ and $M_i -u-> M_j$
$[S_i, M_i] =x=> [S_j, M_j]$	For $x \in L^*$, $S_i =x=> S_j$ and $M_i =x=> M_j$
$[S_i, M_i] \text{-after-} V$	Given a pair of states $[S_i, M_i] \in St_S \times St_M$, and a set $V \subseteq L^*$ $[S_i, M_i] \text{-after-} V = \{[S_j, M_j] \mid \exists x \in L^* (x \in V \ \& \ [S_i, M_i] =x=> [S_j, M_j])\}$
\mathbb{D}	$\mathbb{D} = [S_0, M_0] \text{-after-} L^*$
\mathbb{D}_r	$\mathbb{D}_r = \{[S_i, M_j] \mid [S_i, M_j] \in \mathbb{D} \ \& \ S_i =_w M_j\}$
\mathbb{D}_i	$\mathbb{D}_i = \{[S_k, M_k] \mid [S_k, M_k] \in \mathbb{D}_r \ \& \ S_k \sqsubseteq f(S_i)\}$
\bar{L}_i^k	$\bar{L}_i^k = \{\varepsilon\} \approx Li \approx \dots \approx Li^k$, when $k \in \mathbb{N}$; and $\bar{L}_i^0 = \{\varepsilon\}$.

It is easy to see $\mathbb{D}_r \subseteq \mathbb{D}$ and $|\mathbb{D}_r| \leq |\mathbb{D}| \leq n6m$.

LEMMA 1: For $V \subseteq L^*$, assume $|[S_0, M_0] \text{-after-} V| \leq k$.

If $|\mathbb{D}| > k$, then $|[S_0, M_0] \text{-after-} V.(\{\varepsilon\} \approx Li)| \leq k+1$; and if $|\mathbb{D}| \leq k$, then

$$|[S_0, M_0] \text{-after-} V.(\{\varepsilon\} \approx Li)| = |[S_0, M_0] \text{-after-} V|.$$

Proof:

(I) To prove that the lemma holds when $|\mathbb{D}| > k$.

The lemma holds when $|[S_0, M_0] \text{-after-} V| > k$. Now consider the case that $|[S_0, M_0] \text{-after-} V| = k$.

statements	reasons
(1) $ \mathbb{D} > k$	hypothesis
(2) $ [S_0, M_0] \text{-after-} V = k$	hypothesis
(3) $[S_0, M_0] \text{-after-} V / \mathbb{D}$	definition of \mathbb{D}

- (4) $\exists[S_i, M_i] \square \mathbb{D} \setminus [S_0, M_0] \text{-after-V}$ (1) & (2) & (3)
- (5) $\exists[S_{k-1}, M_{k-1}] \square [S_0, M_0] \text{-after-V}$
 $\exists[S_k, M_k], [S_i, M_i] \square \mathbb{D} \setminus [S_0, M_0] \text{-after-V}$
 $\exists u \square L \exists x, y \square L^*$ such that: $x \text{ in } \square V$ &
 $([S_0, M_0] = x \Rightarrow [S_{k-1}, M_{k-1}] \text{-u-} \Rightarrow [S_k, M_k] = y \Rightarrow [S_i, M_i])$ (4)
- (6) $\exists[S_k, M_k] \square ([S_0, M_0] \text{-after-V} . (\{\varepsilon\} \approx Li)) \setminus [S_0, M_0] \text{-after-V}$ (5)
- (7) $|[S_0, M_0] \text{-after-V} . (\{\varepsilon\} \approx Li)| \varepsilon k + 1$ (6)

(II) To prove that the lemma holds when $|\mathbb{D}| \leq k$.

- (1) $|\mathbb{D}| \leq k$ hypothesis
- (2) $|[S_0, M_0] \text{-after-V}| \varepsilon k$ hypothesis
- (3) $[S_0, M_0] \text{-after-V} / \mathbb{D}$ definition of \mathbb{D}
- (4) $[S_0, M_0] \text{-after-V} . (\{\varepsilon\} \approx Li) = [S_0, M_0] \text{-after-V}$ (1) & (2) & (3). \square

LEMMA 2: Assume $S_0 =_Q M_0$. If $|\mathbb{D}| > \delta 6m$, then $|[S_0, M_0] \text{-after-Q} . \bar{L}_i^{\delta m - n}| \varepsilon \delta 6m$;

and if $|\mathbb{D}| \leq \delta 6m$, then $[S_0, M_0] \text{-after-Q} . \bar{L}_i^{\delta m - n} = \mathbb{D}$.

Proof:

Since $\delta m \geq n$, $\bar{L}_i^{\delta m - n}$ is always defined.

(I) To prove that the lemma holds when $|\mathbb{D}| > \delta 6m$.

- (1) $S_0 =_Q M_0$ hypothesis
- (2) $|\mathbb{D}| > \delta 6m$ hypothesis
- (3) $|[S_0, M_0] \text{-after-Q}| \varepsilon n$ S is initially-connected & (1)
- (4) $|[S_0, M_0] \text{-after-Q} . \bar{L}_i^{\delta m - n}| \varepsilon \delta 6m$ (2) & (3) & apply Lemma 1 $\delta 6m - n$ times

(II) It is evident from Lemma 1 that the lemma also holds when $|\mathbb{D}| \leq \delta 6m$. \square

LEMMA 3: For $S_i \square St_S$, $|\mathbb{D}_i| \leq m$

Proof:

- (1) $|St_M| = m$ hypothesis
- (2) $|\mathbb{D}_i| > m$ assumption

- (3) $\exists [S_j, M_k], [S_l, M_k] \square \mathbb{D}_i (j \square l \ \& \ S_j =_W M_k \ \& \ S_l =_W M_k)$ (1) & (2)
- (4) $S_j =_W S_l$ (3) & M is completely specified
- (5) (4) is not true "definition of W" & " $S_j, S_l \square f(S_i)$ "
- (6) $|\mathbb{D}_i| \leq m$ (2) causes the contradiction between (4) and (5). \square

LEMMA 4: $|\mathbb{D}_r| \leq \delta 6m$.

Proof:

Let $E = \{f(S_i) \mid S_i \square St_S\}$.

- (1) $\delta = |E|$ definition of δ
- (2) $|\mathbb{D}_r / f(S_i) \in E \mathbb{D}_i|$ definition of \mathbb{D}_r
- (3) $\forall f(S_i) \square E (|\mathbb{D}_i| \leq m)$ Lemma 3
- (4) $|\mathbb{D}_r| \leq \sum_{f(S_i) \in E} |\mathbb{D}_i|$ (2)
- (5) $|\mathbb{D}_r| \leq \delta 6m$ (1) & (3) & (4). \square

LEMMA 5: If $S_0 =_{\square 1} M_0$, then $[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n} = \mathbb{D}_r$.

Proof:

When $|\mathbb{D}| \leq \delta 6m$, the lemma is evident from Lemma 2. Now consider the case that $|\mathbb{D}| > \delta 6m$.

- (1) $S_0 =_{\square 1} M_0$ hypothesis
- (2) $|\mathbb{D}| > \delta 6m$ hypothesis
- (3) $|[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n}| \leq \delta 6m$ (2) & Lemma 2
- (4) $[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n} / \mathbb{D}_r$ (1)
- (5) $|[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n}| \leq |\mathbb{D}_r| \leq \delta 6m$ (4) & Lemma 4
- (6) $|[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n}| = |\mathbb{D}_r| = \delta 6m$ (3) & (5)
- (7) $[S_0, M_0] \text{-after-Q} \cdot \bar{L}_i^{\delta m - n} = \mathbb{D}_r$ (4) & (6). \square

LEMMA 6: If $S_0 =_{\square 1} M_0$, then $\forall [S_i, M_k] \square \mathbb{D} (\exists [S_j, M_k] \square \mathbb{D}_r)$.

Proof:

Let $E = \{f(S_i) \mid S_i \sqsubseteq St_S\}$, thus $\delta = |E|$.

- (1) $S_0 =_{\square 1} M_0$ hypothesis
- (2) $S_0 =_Q M_0$ (1)
- (3) if $|\mathbb{D}| > |\llbracket S_0, M_0 \rrbracket\text{-after-V}|$,
 then $|\llbracket S_0, M_0 \rrbracket\text{-after-V} \cdot (\{\varepsilon\} \approx Li)| \varepsilon |\llbracket S_0, M_0 \rrbracket\text{-after-V}| + 1$ the same reason as for Lemma 1
- (4) $|\llbracket S_0, M_0 \rrbracket\text{-after-Q}| \varepsilon n$ "S is initially-connected" & (2)
- (5) $\text{not}(\forall [S_i, M_k] \sqsubseteq \mathbb{D} (\exists [S_j, M_k] \sqsubseteq \mathbb{D} r))$ assumption
- (6) $\llbracket S_0, M_0 \rrbracket\text{-after-Q} \cdot \bar{L}_i^{\delta m - n} \mathbb{D} r \mathbb{D} \ \& \ \mathbb{D} r \sqsubseteq \mathbb{D}$ (1) & (5)
- (7) $|\llbracket S_0, M_0 \rrbracket\text{-after-Q} \cdot \bar{L}_i^{\delta m - n}| \varepsilon \delta 6m$ (4) & (6) & "apply (3) $\delta m - n$ times"
- (8) $|\mathbb{D} r| \varepsilon \delta 6m$ (6) & (7)
- (9) $\exists M_1 \sqsubseteq St_M \forall [S_i, M_j] \sqsubseteq \mathbb{D} r (l \sqcup j)$ (5)
- consider such a M_1 make a convention
- \cup
- (10) $\mathbb{D} r \setminus f(S_i) \in E \ \mathbb{D}_i$ definition of $\mathbb{D} r$
- (11) $\forall f(S_i) \in E (|\mathbb{D}_i| \leq m - 1)$ (9) & the similar reason for Lemma 3
- (12) $|\mathbb{D} r| \leq \sum_{f(S_i) \in E} |\mathbb{D}_i|$ (10)
- (13) $|\mathbb{D} r| \leq \delta 6(m - 1)$ (11) & (12) & $\delta = |E|$.
- (14) $\forall [S_i, M_k] \sqsubseteq \mathbb{D} (\exists [S_j, M_k] \sqsubseteq \mathbb{D} r)$ (5) causes the contradiction between (8) and (13). \square

LEMMA 7: If $S_0 =_{\square 1} M_0$, then $\forall [S_i, M_k] \sqsubseteq \mathbb{D} ([S_i =_{w_i} M_k] \iff [S_i =_w M_k])$.

Proof:

- (1) $S_0 =_{\square 1} M_0$ hypothesis
- (2) $[S_i, M_k] \sqsubseteq \mathbb{D} \ \& \ S_i =_{w_i} M_k$ assumption
- (3) $S_j =_w M_k$ (2) & (1) & Lemma 6
- (4) $S_i =_{w_i} S_j$ (2) & (3) & $W_i \dot{\text{pref}}(W)$
- (5) $i = j$ (4) & definition of W_i
- (6) $\forall [S_i, M_k] \sqsubseteq \mathbb{D} ([S_i =_{w_i} M_k] \implies [S_i =_w M_k])$ (2) \implies (3) & (5)

- (7) $\forall [S_i, M_k] \square \mathbb{D} ([S_i =_{W_i} M_k] \iff [S_i =_W M_k])$ definition of W_i
- (8) $\forall [S_i, M_k] \square \mathbb{D} ([S_i =_{W_i} M_k] \iff [S_i =_W M_k])$ (6) & (7). \square

LEMMA 8: If $S_0 =_{\square} M_0$, then $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n} = \mathbb{D}_r = \mathbb{D}$.

Proof:

- (1) $S_0 =_{\square} M_0$ hypothesis
- (2) $S_0 =_{\square 1} M_0$ (1)
- (3) $S_0 =_{\square 2} M_0$ (1)
- (4) $S_0 =_{\mathbb{Q}} M_0$ (1)
- (5) $[S_0, M_0] \text{-after-} \mathbb{R}. L_i^{\delta m - n} / \mathbb{D}_r$ (3) & (2) & Lemma 7
- (6) $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n + 1} / \mathbb{D}_r$ (5) & (2) & $\mathbb{R} \approx \mathbb{Q} = \mathbb{Q}. (\{\varepsilon\} \approx L_i)$
- (7) $|\mathbb{D}| > \delta m$ assumption
- (8) $|[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n + 1}|_{\varepsilon \delta m + 1}$ (7) & (4) & Lemma 2 & Lemma 1
- (9) (7) is not true (6) & Lemma 3
- (10) $|\mathbb{D}| \leq \delta m$ (7) causes the contradiction between (7) and (9)
- (11) $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n + 1} = \mathbb{D}$ (10) & (4) & Lemma 2
- (12) $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n + 1} = \mathbb{D}_r = \mathbb{D}$ (6) & (11) & $\mathbb{D}_r \mathbb{D}$
- (13) $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n} = \mathbb{D}_r = \mathbb{D}$ (12) & Lemma 5. \square

LEMMA 9: If $S_0 =_{\square} M_0$, then $S_0 \leq_{\text{quasi}} M_0$.

Proof:

Note that $[S_0, M_0] \text{-after-} \mathbb{Q}. \bar{L}_i^{\delta m - n + 1} = [S_0, M_0] \text{-after-} \mathbb{P}. \bar{L}_i^{\delta m - n}$.

- (1) $S_0 =_{\square} M_0$ hypothesis
- (2) $\forall x \square L^*(\text{ if } x \text{ in } \square \mathbb{Q}. \bar{L}_i^{\delta m - n} \text{ and } [S_0, M_0] =_x \Rightarrow [S_j, M_j],$
then (i) $[S_j, M_j]$ is unique, and
(ii) $\forall a \square L_i (S_j =_{\{a\}} M_j)$) (1) & Lemma 8
- (3) not $(S_0 \leq_{\text{quasi}} M_0)$ assumption

- (4) $\exists y \sqsubseteq L^* \exists u \sqsubseteq L \exists [S_i, M_i] \sqsubseteq \mathbb{D}r$ such that $y \text{in} \sqsubseteq \mathbb{Q} \cdot \bar{L}_i^{\delta m-n}$ &
 $[S_0, M_0] = y \Rightarrow [S_i, M_i] \& S_i \text{-} u \text{-} \rightarrow \& M_i \setminus \text{-} u \text{-} \rightarrow$ (3) & (1) & Lemma 8 &
- (5) $S_0 \leq_{\text{quasi}} M_0$ (3) causes the contradiction between (2) and (4). \square

LEMMA 10: $S_0 =_{\sqsubseteq} M_0$ iff $S_0 =_{\sqsubseteq} I_0$.

Proof: Since $I_0 =_{\sqsubseteq} M_0$, $S_0 =_{\sqsubseteq} M_0$ implies $S_0 =_{\sqsubseteq} I_0$. By the same reason, $S_0 =_{\sqsubseteq} I_0$ implies $S_0 =_{\sqsubseteq} M_0$. \square

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